

The generalized amalgamation of any graph whose terminal is a subgraph admits a super H-antimagic Total Covering

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Abstract

Let $\{H_i\}$ be a finite collection of a simple connected graph, and suppose each H_i has a fixed vertex $v \in V(H_i)$ as a terminal. The amalgamation H_i of v as a terminal is constructed by taking all the H_i 's positif integer n , we denote such amalgamation by $G = \text{amal}(H, n)$, where n denotes the number of copies of H . If we replace the terminal vertex v by a subgraph $K \subseteq H$ then such amalgamation is said to be a generalized amalgamation of G and denoted by $G = \text{gamal}(H, K \subseteq H, n)$. A graph G is said to be an (a, d) - H -antimagic total graph if there exist a bijective function $f : V(G) \cup E(G) \rightarrow \{1, 2, \dots, |V(G)| + |E(G)|\}$ such that for all subgraphs isomorphic to H , the total H -weights $W(H) = \sum_{v \in V(H)} f(v) + \sum_{e \in E(H)} f(e)$ form an arithmetic sequence $\{a, a + d, a + 2d, \dots, a + (n - 1)d\}$, where a and d are positive integers and n is the number of all subgraphs isomorphic to H . If such a function exist then f is called an (a, d) - H -antimagic total labeling of G . An (a, d) - H -antimagic total labeling f is called super if the smallest labels appear in the vertices. In this paper, we study the existence of super (a, d) - H -antimagic total labeling of is called super if the smallest labels appear in the vertices. In this paper, we study a super (a, d) - H antimagic total labeling $G = \text{gamal}(H, K \subseteq H, n)$ for both connected and disconnected graphs by implementing a partition techniques. The result shows that the generalized amalgamation of any graph H whose terminal is a subgraph admits super H -antimagic total covering for almost feasible difference d .

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