

# ICMIs 2018

The 1st International Conference on Mathematics and Islam

## Proceedings

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Mataram, Nusa Tenggara Barat, Indonesia

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ADMAPETA  
Asosiasi Dosen Matematika dan  
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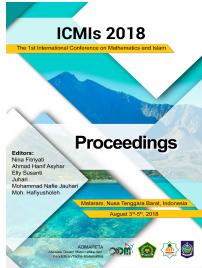
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## Proceedings

### Proceedings of the International Conference on Mathematics and Islam

August 3-5, 2018, in Mataram, Indonesia

**Editors:** Nina Fitriyati <sup>1</sup>; Ahmad Hanif Asyhar <sup>2</sup>; Elly Susanti <sup>3</sup>; Juhari <sup>3</sup>; Mohammad Nafie Jauhari <sup>3</sup> and Moh. Hafiyusholeh <sup>3</sup>**Affiliations:** <sup>1</sup> Universitas Islam Negeri Syarif Hidayatullah Jakarta, Indonesia ; <sup>2</sup> Universitas Islam Negeri Sunan Ampel Surabaya, Indonesia ; <sup>3</sup> Universitas Islam Negeri Maulana Malik Ibrahim Malang, Indonesia**ISBN:** 978-989-758-407-7**Conference Link:** <http://conferences.ad-apsmapeta.or.id/>

**Foreword:** The 1st International Conference on Mathematics and Islam (ICMIs 2018) is an academic event held by UIN Mataram Indonesia and ADMAPETA (Asosiasi dosen matematika dan pendidikan/Tadris Matematika). This event was held on August 3rd-5th, 2018 in Mataram, Nusa Tenggara Barat, Indonesia. the theme of the conference is "Contextualization of Mathematics Through Islamic Values Integration". The Organizing committee have successfully compiled articles written by scholars, researchers, experts and those who have keen interests in mathematics, applied mathematics, mathematics education, Integration of Mathematics and Islam. Mathematics as logical thinking methods and tools is used to help a person solve problems that occur in surrounding environment. Those happens because generally, education accommodating the complete form of human, a human who can maximize their potential for self-interest also for their community. Integration between Islamic values and Mathematics can help achieve its goal. Contextual value of Islam in Mathematics is a process of developing students in Mathematics skills through Islamic values. Besides as the basic design of learning, Islamic values can be proven perfectly through mathematical thinking and media learning Mathematics. Such as used study case that has Islamic values to teach Mathematics. The aim of the first International conference are building common frame of mind, the work scheme, and the standard format for Mathematics lecturer or Mathematics Education lecturer in PTKI and developing Islamic value based on Mathematics learning. The event is held because of the concept of education that organized by the government based on SISDIKNAS. SISDIKNAS is a learning method that developing students to understanding their material and to gaining the characteristics according to the national identity of Indonesia, based on religious values. ([Less](#))

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**On inclusive 1-Distance Vertex Irregularity Strength of Firecracker, Broom, and Banana Tree**

In Proceedings of the International Conference on Mathematics and Islam - ICMIs, 228-232, 2018 , Mataram, Indonesia

**On inclusive 1-Distance Vertex Irregularity Strength of Firecracker, Broom, and Banana Tree**

Iksanul Halikin<sup>1</sup>, Ade Rizky Savitri<sup>2</sup> and Kristiana Wijaya<sup>3</sup>  
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**Keywords:** Inclusive 1-Distance Vertex Irregular Labelling, Inclusive 1-Distance Vertex Irregular Strength.

**Abstract:** Let k be a natural number and G be a simple graph. An inclusive d-distance vertex irregular labelling of a graph G is a function  $\lambda: V(G) \rightarrow \{1, 2, \dots, k\}$  so that the weights at each vertex are different. Let v be a vertex of G. The weight of  $v \in V(G)$ , denoted by  $wt(v)$ , is the sum of the label of v and all vertex labels up to distance 1 from v. The inclusive 1-distance vertex irregular strength of G, denoted by  $\text{is}(G)$ , is the minimum k for the existence of an inclusive 1-distance vertex irregular labelling of a G. Here, we find the exact value of an inclusive 1-distance vertex irregularity strength of a firecracker, a broom, and banana tree.

**1 INTRODUCTION**

Suppose that G is an undirected and finite graph without loop and parallel edges. For a vertex  $v$  in a graph G, let  $N(v)$  denote the set of vertices in G that are incident to  $v$ . For two vertices  $u$  and  $v$  in a graph G (not necessarily distinct), the distance between  $u$  and  $v$  is the number of vertices and edges in G, starting with  $u$  and ending with  $v$ , such that every two consecutive vertices in the path are adjacent. A path defined as  $u = u_0$  – walk with length 0. If there is a path from  $u$  to  $v$ , then  $v$  is said to be a distance  $n$  vertex from  $u$  and  $u$  is said to be a distance  $n$  vertex from  $v$  (see Chartrand, Lesniak & Pólya (2011) for a complete survey).

The labeling in graph is one of research topics in mathematics. There are many types of labeling functions from a set of graph elements (vertices or edges) to a set of integers (natural numbers or even numbers) with certain conditions. There are many types of labeling in graphs, such as total labeling (see Gallian (2016) for a complete survey). Chellali et al. (2017) introduced the concept of an irregular labeling in 1988. The problem of determining the irregularity strength of a graph is how to assign natural numbers label to the edges of a graph such that the sum of the labels of the edges incident to a vertex is different. In this labeling also introduced a notion, called irregularity strength, i.e. the minimum largest

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 Halikin, I., Savitri, A. and Wijaya, K. (2020). On inclusive 1-Distance Vertex Irregularity Strength of Firecracker, Broom, and Banana Tree. In *Proceedings of the International Conference on Mathematics and Islam - ICMIs*, ISBN 978-989-758-407-7, pages 228-232. DOI: 10.5220/0008519802280232

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**Keyword(s):** Inclusive 1-Distance Vertex Irregular Labelling, Inclusive 1-Distance Vertex Irregularity Strength, Firecracker, Broom, and Banana Tree.

**Abstract:** Let k be a natural number and G be a simple graph. An inclusive d-distance vertex irregular labelling of a graph G is a function so that the weights at each vertex are different. Let v be a vertex of G. The weight of  $v \in V(G)$ , denoted by  $wt(v)$ , is the sum of the label of v and all vertex labels up to distance 1 from v. An inclusive 1-distance vertex irregularity strength of G, denoted by  $\text{is}(G)$ , is the minimum k for the existence of an inclusive 1-distance vertex irregular labelling of a G. Here, we find the exact value of an inclusive 1-distance vertex irregularity strength of a firecracker, a broom, anda banana tree.



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# On inclusive 1-Distance Vertex Irregularity Strength of Firecracker, Broom, and Banana Tree

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**Keywords:** Inclusive 1-Distance Vertex Irregular Labelling, Inclusive 1-Distance Vertex Irregularity Strength, Firecracker, Broom, Banana Tree.

**Abstract:** Let  $k$  be a natural number and  $G$  be a simple graph. An *inclusive  $d$ -distance vertex irregular labelling* of a graph  $G$  is a function  $\lambda: V(G) \rightarrow \{1, 2, \dots, k\}$  so that the weights at each vertex are different. Let  $v$  be a vertex of  $G$ . The weight of  $v \in V(G)$ , denoted by  $wt(v)$ , is the sum of the label of  $v$  and all vertex labels up to distance 1 from  $v$ . An *inclusive 1-distance vertex irregularity strength* of  $G$ , denoted by  $\widehat{dis}(G)$  is the minimum  $k$  for the existence of an inclusive 1-distance vertex irregular labelling of a  $G$ . Here, we find the exact value of an inclusive 1-distance vertex irregularity strength of a firecracker, a broom, and a banana tree.

## 1 INTRODUCTION

Suppose that  $G$  is an undirected and finite graph without loop and parallel edges. For a vertex  $v$  in a graph  $G$ , the degree of  $v$  with notation  $d(v)$  is the number of edges in  $G$  that are incident to  $v$ . For two vertices  $u$  and  $v$  in a graph  $G$  (not necessarily distinct), a  $u - v$  walk in  $G$  is defined as a sequence of vertices and edges in  $G$ , starting with  $u$  and ending at  $v$  such that consecutive vertices are connected by an edge. A path defined as a  $u - v$  walk with different vertices. The length of the shortest path from vertex  $u$  to vertex  $v$  is said to be a distance from  $u$  to  $v$  and denoted by  $d(u, v)$  (see Chartrand, Lesniak & Zhang, (2011) for another terminology).

The labelling in graph is one of research topics introduced in the 1960s. The labelling of a graph is a function from a set of graph elements (vertices or edges or both) onto a set of numbers (usually natural numbers) with certain condition. There are many kinds of graph labelling that have been introduced (see Gallian (2016) for a complete survey). Chartrand et al. suggested the concept of an irregular labelling in 1988. The problem of this labelling is how to assign natural numbers label to the edges of a graph so that the sum of edge labels at each vertex is different. In this labelling also introduced a notion, called irregularity strength, i.e. the minimum largest

label among all of the possible irregular assignments of a graph (Chartrand et al., 1988).

In 2007, Bačá et al. introduced the similar assignment but apply to both edges and vertices of a graph. This labelling is called the irregular total  $k$ -labelling. A total  $k$ -labelling is a mapping from the vertex set and edge set to the set of natural numbers  $\{1, 2, \dots, k\}$ . The minimum  $k$  for such labelling is said to be the total irregularity strength. Furthermore, Mirka, Rodger & Simanjuntak (2003) introduced another kind labelling, which is called distance magic labelling.

Motivated by Mirka and Bačá, Slamin (2017) introduced a distance vertex irregular labelling of graphs. A *distance vertex irregular labelling* of a graph  $G$  is a function  $\lambda: V(G) \rightarrow \{1, 2, \dots, k\}$  such that the weight of every vertex  $v$  in  $G$  is different. The weight of a vertex  $v \in V(G)$ , denoted by  $wt(v)$ , is the sum of the labels of all the vertices of distance 1 from  $v$ . Moreover, Bong, Lin & Slamin (2017), generalized concept of a distance irregular vertex labelling to *inclusive* vertex irregular  $d$ -distance vertex labelling. Inclusive in this labelling means that the weight of the vertex  $v$  included the label of a vertex  $v$ . The minimum  $k$  for the existence of this labelling is said to be a *distance irregularity strength* of  $G$  and denoted by  $\widehat{dis}_d(G)$ . Furthermore, Bong, Lin & Slamin (2017) obtained  $\widehat{dis}(G)$ , for  $G$  are a path  $P_n$  for  $n = 3k$ ,  $k \in \mathbb{N}$ , a star  $K_{1,n}$ , and a double

star  $S(m, n)$  with  $m \leq n$ . In the same paper, they gave the lower bound for caterpillar, cycle and wheel. In 2018, Baća et al. determined the exact value of the inclusive distance vertex irregularity strength of a complete graph, complete bipartite graph, path, fan, and cycle.

In this paper, we discuss an inclusive 1-distance vertex irregular labelling and find the exact value of an inclusive 1-distance vertex irregularity strength of a firecracker, broom, and banana tree.

## 2 DEFINITION AND USEFUL PROPERTIES

Before we start the further discussion, we will present the definition and some useful properties of an inclusive 1-distance vertex irregular labelling.

**Definition 1.** Let  $k$  be a natural number. An *inclusive  $d$ -distance vertex irregular labelling* of a graph  $G$  is a function  $\lambda: V(G) \rightarrow \{1, 2, \dots, k\}$  so that the weights of two vertices  $u$  and  $v$  are different for each  $u, v \in V(G)$ . The weight of a vertex  $v \in V(G)$ , denoted by  $wt(v)$ , is defined as the sum of the label of  $v$  and all vertex labels up to distance  $d$  from  $v$ , namely

$$wt(v) = \lambda(v) + \sum_{1 \leq d(u,v) \leq d} \lambda(u),$$

where  $d(u, v)$  is distance from vertex  $u$  to  $v$ .

The smallest  $k$  for the largest labelling this labelling is called an *inclusive  $d$ -distance irregularity strength* of  $G$  and denoted by  $\widehat{dis}_d(G)$ . Since in this paper we take  $d = 1$ , we denote it with  $\widehat{dis}(G)$ . Not all graphs  $G$  have an inclusive 1-distance irregularity strength of  $G$ , and we say that  $\widehat{dis}(G) = \infty$ .

Bong, Lin & Slamin (2017), gave the lower bound of the inclusive 1-distance irregularity strength of  $G$ , by the following lemma.

**Lemma 1.** For a connected graph  $G$  with  $n$  vertices,  $\delta, \Delta$  as minimum and maximum degree, respectively then  $\widehat{dis}(G) \geq \lceil \frac{n+\delta}{\Delta+1} \rceil$ .

Next, Baća et al. (2018) proved the sufficient and necessary condition for  $\widehat{dis}(G) = \infty$ .

**Lemma 2.** For a connected graph  $G$ ,  $\widehat{dis}(G) = \infty$  if and only if there exist two different vertices  $u, v \in V(G)$  such that  $\{u\} \cup N(u) = \{v\} \cup N(v)$ , where

$N(u)$  is the set of all neighborhood of  $u$ (distance 1 from  $u$ ).

As the firecracker, broom, and banana graphs are the kind of the tree graph, that clearly not satisfy the Lemma 2, so we can find the inclusive 1-distance vertex irregular labelling of them. The definition of firecracker, broom, and banana tree graphs are as follow:

**Definition2.** A firecracker graph  $F_{n,m}$  is a graph formed by connecting one vertex of degree one from each of  $n$  copies of a star  $K_{1,m}$ .

**Definition3.** A broom  $Br_{n,m}$  is a graph formed from identifying one end leaf of a path  $P_n$  with the center of a star  $K_{1,m}$ .

**Definition4.** A banana tree  $B_{n,m}$  is a graph obtained from connecting one vertex of degree one from each of  $n$  copies of a star  $K_{1,m}$  with a new vertex.

In this paper, we determine an inclusive 1-distance vertex irregularity strength of a firecracker  $F_{n,3}$ , a broom  $Br_{3,m}$ , and a banana tree  $B_{2,m}$ .

## 3 MAIN RESULTS

In this section, we discuss an inclusive 1-distance irregularity strength of firecracker  $F_{n,3}$ , broom  $Br_{3,m}$ , and banana tree  $B_{2,m}$ .

**Theorem 1.** Let  $F_{n,3}$  be a firecracker graph with  $n \geq 3$ . Then  $\widehat{dis}(F_{n,3}) = n + 1$ .

Proof. Suppose  $V(F_{n,3}) = \{v_{ij} \mid 1 \leq i \leq 4, 1 \leq j \leq n\}$  where  $d(v_{1j}) = 3$ ,  $d(v_{2j}) = d(v_{3j}) = 1$ , and  $d(v_{41}) = d(v_{4n}) = 2$ , and for  $j \neq 1, 2$ ,  $d(v_{4j}) = 3$ . As illustration, the vertex notation of  $F_{n,3}$  can be seen in Figure 1.

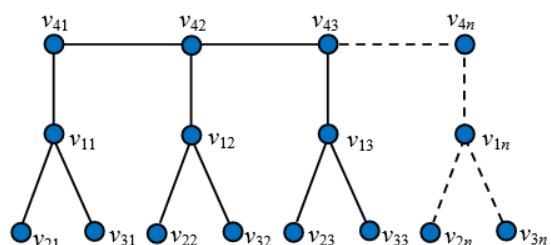


Figure 1: The notation of vertices of a firecracker  $F_{n,3}$ .

We know that a firecracker  $F_{n,3}$  has  $4n$  vertices,  $\Delta(F_{n,3}) = 3$  and  $\delta(F_{n,3}) = 1$ . Based on Lemma 1, we get

$$\widehat{dis}(F_{n,3}) \geq \left\lceil \frac{4n+1}{3+1} \right\rceil = n+1.$$

To show that  $\widehat{dis}(F_{n,3}) \leq n+1$ , we define an inclusive irregular 1-distance vertex labelling  $\lambda$  of  $F_{n,3}$  with label  $1, 2, \dots, n+1$  as follow:

$$\lambda(v_{ij}) = \begin{cases} j+1, & \text{for } i = 1; 1 \leq j \leq n, \\ 1, & \text{for } i = 2; 1 \leq j \leq n-2, \\ 2, & \text{for } i = 2; n-1 \leq j \leq n, \\ n-1, & \text{for } i = 3; j = 1, \\ n+1, & \text{for } i = 3; 2 \leq j \leq n, \\ n+1, & \text{for } i = 4; 1 \leq j \leq n. \end{cases}$$

So, the vertices weight of  $F_{n,3}$  are

$$wt(v_{ij}) = \begin{cases} 2n+3, & \text{for } i = 1; j = 1, \\ 2n+6, & \text{for } i = 1; j = 2, n \geq 4, \\ 2n+4+j, & \text{for } i = 1; 3 \leq j \leq n-2, n \geq 5, \\ 2n+j+5, & \text{for } i = 1; n-1 \leq j \leq n, \\ 3, & \text{for } i = 2; j = 1, \\ j+2, & \text{for } i = 2; 2 \leq j \leq n-2, n \geq 4, \\ j+3, & \text{for } i = 2; n-1 \leq j \leq n, \\ n+1, & \text{for } i = 3; j = 1, \\ n+j+2, & \text{for } i = 3; 2 \leq j \leq n, \\ 2n+4, & \text{for } i = 4; j = 1, \\ 3n+j+4, & \text{for } i = 4; 2 \leq j \leq n-1, \\ 3n+3, & \text{for } i = 4; j = n. \end{cases}$$

We obtain that all vertices of a graph  $F_{n,3}$  have distinct weight. Hence,  $\widehat{dis}(F_{n,3}) \leq n+1$ . Therefore, we can conclude that  $\widehat{dis}(F_{n,3}) = n+1$ . ■

**Theorem 2.** Let  $Br_{3,m}$  be a broom with  $m \geq 2$ , then  $dis(Br_{3,m}) = m$ .

**Proof.** Suppose that  $V(Br_{3,m}) = \{u_i, v_j | 1 \leq i \leq 3, 1 \leq j \leq m\}$  is the vertex set of a broom  $Br_{3,m}$ , where the vertices  $u_1$  and  $v_j$  are leaves of a broom  $Br_{3,m}$  for each  $j \in [1, m]$  and  $u_3$  is the vertex of degree  $m+1$  (see Figure 2). Then, the broom  $Br_{3,m}$  has  $m+1$  leaves. So, all leaves of a broom  $Br_{3,m}$  must have distinct weight, where  $wt(u_1) = \lambda(u_1) + \lambda(u_2)$  and  $wt(v_j) = \lambda(u_3) + \lambda(v_j)$ . Obviously that the smallest weight of a leaf of a broom  $Br_{3,m}$  is at least 2 and minimum of the largest weight of a leaf of a broom  $Br_{3,m}$  is at least  $m+2$ . To obtain distinct weight of leaves  $v_j$ , the leaves  $v_j$  must have different label for each  $j \in [1, m]$ . Hence, minimum

of the largest label of leaves from a broom  $Br_{3,m}$  is at least  $m$ . It means that  $\widehat{dis}(Br_{3,m}) \geq m$ .

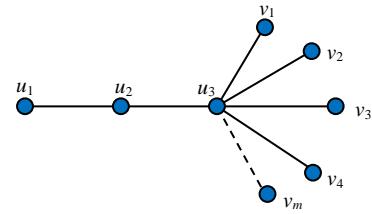


Figure 2: The notation of vertices of a broom  $Br_{3,m}$ .

Now, we show that  $\widehat{dis}(Br_{3,m}) \leq m$ . We define the inclusive irregular 1-distance vertex labelling  $\lambda$  as follow,

$$\lambda(v_j) = j, \text{ for } 1 \leq j \leq m, \\ \lambda(u_i) = \begin{cases} m, & \text{for } i = 1, \\ 4-i, & \text{for } 2 \leq i \leq 3. \end{cases}$$

So, the corresponding weights of each vertex of a broom  $Br_{3,m}$  are

$$wt(v_j) = j+1, \text{ for } 1 \leq j \leq m,$$

$$wt(u_i) = \begin{cases} m+1+i, & \text{for } 1 \leq i \leq 2, \\ \frac{1}{2}(m^2+m+6), & \text{for } i = 3. \end{cases}$$

The differences of every vertex weight in a broom graph  $Br_{3,m}$  can be verified easily. Since the largest label of a vertex of a broom  $Br_{3,m}$  is at most  $m$ ,  $\widehat{dis}(Br_{3,m}) \leq m$ . Therefore, we can conclude that  $\widehat{dis}(Br_{3,m}) = m$ . ■

**Theorem 3.** Let  $B_{2,m}$  be a banana tree with  $m \geq 3$ , then

$$\widehat{dis}(B_{2,m}) = \begin{cases} 4, & \text{for } m = 3, \\ m, & \text{for } m \geq 4. \end{cases}$$

**Proof.** Let  $V(B_{2,m}) = \{z, x_i, y_i | 0 \leq i \leq m\}$  be the vertex set of a banana tree  $B_{2,m}$ , where the only two vertices adjacent to  $z$  are  $x_1$  and  $y_1$ ,  $d(x_0) = d(y_0) = m$ , and the others are leaves. The notation of vertices of a banana tree  $B_{2,m}$  as depicted in Figure 3. First, we will find the lower bound of the inclusive 1-distance irregularity strength for a banana tree  $B_{2,m}$ . To find this, we consider 2 cases.

**Case1.** For  $m = 3$

Suppose the vertex set of a banana tree  $B_{2,3}$  is  $V(B_{2,3}) = \{z, x_i, y_i | i = 0, 1, 2, 3\}$ . A banana tree  $B_{2,3}$

has 4 leaves, namely  $x_1, x_2, y_1, y_2$ . The smallest weight of a leaf of a banana tree  $B_{2,3}$  is at least 2, and minimum of the largest weight of a leaf of a banana tree  $B_{2,3}$  is at least 5. So, the label of each leaf is at least  $\lceil \frac{5}{2} \rceil = 3$ . Without loss of generality, it causes  $\lambda(x_0) = 1$  and  $\lambda(y_0) = 2$ . However, minimum of the largest weight of all vertices of a banana tree  $B_{2,3}$  is at least 10. If the largest vertex label of a banana tree  $B_{2,3}$  is 3, then the vertex with weight 10 should be  $y_0$ . It cause  $\lambda(y_1) = 3$  and the possibility of weight of  $y_1$  is either 6, 7, or 8. On the other hand, the possibility of weight of  $x_0$  is either 6 or 7. Two possibilities of weight of  $x_0$  will cause two of vertices  $z, x_0, x_1$ , and  $y_1$  have the same weight. Hence, the largest label of each vertex of a banana tree  $B_{2,3}$  is at least 4. So,  $\widehat{dis}(B_{2,3}) \geq 4$ .

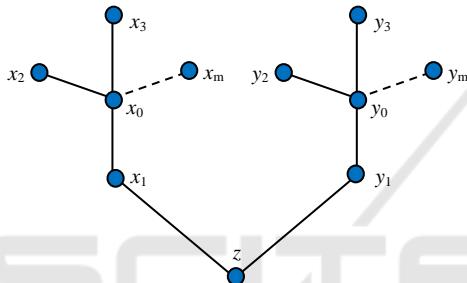


Figure 3: The notation of vertices of a banana tree  $B_{2,m}$ .

To show that  $\widehat{dis}(B_{2,3}) \leq 4$ , we can label of a banana tree  $B_{2,3}$  as depicted in Figure 4.

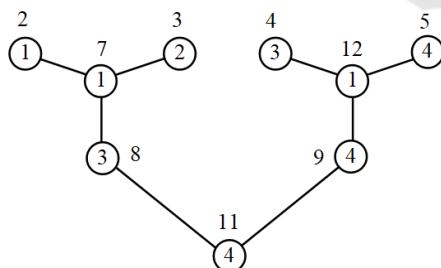


Figure 4: The labelling of banana tree  $B_{2,3}$ .

Figure 4 shows the inclusive irregular 1-distance vertex labelling, where the number outside the cycle shows the weight of the given vertex.

#### Case2. For $m \geq 4$

A banana tree  $B_{2,m}$  has  $(2m - 2)$  leaves. The smallest weight of a leaf of a  $B_{2,m}$  is at least 2 and minimum of the largest weight of a leaf of a  $B_{2,m}$  is at least  $2m - 1$ . So, minimum of the largest leaf

label of a banana tree  $B_{2,m}$  is at least  $\lceil \frac{2m-1}{2} \rceil = m$ . Meanwhile, minimum of the largest weight for every vertex of a graph  $B_{2,m}$  is at least  $2m + 4$ . Therefore, minimum of the largest vertex label of a banana tree  $B_{2,m}$  is at least  $\min\{\lceil \frac{2m-1}{2} \rceil, \lceil \frac{2m+4}{2} \rceil\} = m$ . So,  $\widehat{dis}(B_{2,m}) \geq m$ .

To show that  $\widehat{dis}(B_{2,m}) \leq m$ , let the inclusive irregular 1-distance vertex labelling  $\lambda$  is defined in the following way:

$$\lambda(z) = m$$

$$\lambda(y_i) = \begin{cases} m-1, & \text{for } i = 0 \\ m, & \text{for } i = 1 \\ i, & \text{for } 2 \leq i \leq m \end{cases}$$

So, the corresponding weights of each vertex of a banana tree  $B_{2,m}$  are as follows.

$$wt(z) = 3m$$

$$wt(x_i) = \begin{cases} \frac{1}{2}(m^2 + m + 2), & \text{for } i = 0 \\ 2m + 1, & \text{for } i = 1 \\ i, & \text{for } 2 \leq i \leq m \end{cases}$$

$$wt(y_i) = \begin{cases} \frac{1}{2}(m^2 + 5m - 4), & \text{for } i = 0 \\ 3m - 1, & \text{for } i = 1 \\ m + i - 1, & \text{for } 2 \leq i \leq m \end{cases}$$

The differences of every vertex weight can be verified easily, and the largest label is  $m$ . So,  $\widehat{dis}(B_{2,m}) \leq m$ . Therefore, we can conclude that  $\widehat{dis}(B_{2,m}) = m$ . ■

For example, the inclusive irregular 1-distance vertex labelling of a banana tree  $B_{2,4}$  can be seen in Figure 5.

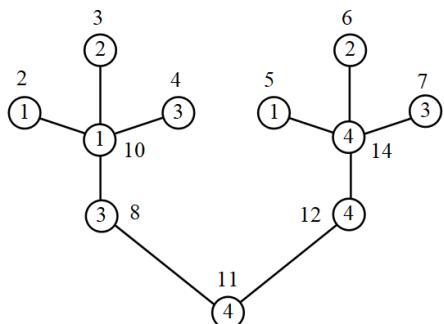


Figure 5: The labelling of banana tree  $B_{2,4}$ .

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