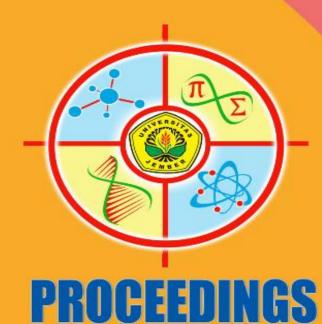
ISBN: 978-602-60569-5-5





The 1st International Basic Science Conference 2016
TOWARDS THE EXTENDED USE OF BASIC SCIENCE
FOR ENHANCING HEALTH, ENVIRONMENT,
ENERGY, AND BIOTECHNOLOGY

University of Jember, September 26 - 27, 2016





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Proceeding of 1st International Basic Science Conference (1st-IBSC) 2016

ISBN: 978-602-60569-5-5

Presented articles on proceeding 1st International Basic Science Conference

"Towards The Extended Use Of Basic Science For Enhancing Health, Environment, Energy, And Biotechnology"

26-27th September 2016, University of Jember, Indonesia

PUBLISHED: 2017-08-22

GENERAL

Community Strategy for Managing Tropical Forest Resources in The Areaof Cagar Alam Pulau Sempu (Nature Reserve of Sempu Island)

Lely Mardiyanti, Rifalatul Isnaini, Sueb Sueb 2-6



BIOREDUCTION ADSORBENT (BIOSORBENT): RECOVERY TECHNOLOGY OF HEAVY METAL POLLUTION (CADMIUM/CD) IN POLLUTED LAPINDO WATER SOURCES USING BACTERIA AND DURIAN LEATHER

Sueb Sueb, Eka Imbia Agus Diartika, Khasanah Sripalupi, Achib Irmawati 7-9



COMPARATIVE STUDY OF THE MANAGEMENT OF VANAME SHRIMP (LITOPENAEUS VANNAMEI) BASED ON DEMOGRAPHIC FACTORS AT MOLANG BEACH TULUNGAGUNG

Firda Ama Zulfia, Ika Airin Nur Rohmadhani, Nova Yesika Gultom, Sueb Sueb



ANALYSIS OF THE INFLUENCE OF PUBLIC PARTICIPATION IN THE MANAGEMENT OF RESOURCES SUSTAINABLE WATER MALANG DISTRICT

Ahmad Kamal Sudrajat, Dewi Nur Arasy, Daning Nindya Fitri Arianti, Sueb Sueb 13-15



CONSERVATION COCCINELLA SP. AS PREDATOR OF GREEN PEACH APHID MYZUS PERSICAE SULZER ON POTATO INTERCROPPING

Lamria Sidauruk

16-18



THE EFFECT OF MYCORRHIZAL INOCULANT AND COMPOST OF VOLCANIC ASH ON GROWTH AND YIELD OF CHILLI (CAPSICUM ANNUM L.)

Ernitha Panjaitan, Nur Syntha Napitupulu, Ezra Matondang 19-22



THE POTENTIAL OF ARTHROPODE DIVERSITY FOR ECOTOURISM DEVELOPMENT IN WONOREJO MANGROVE ECOSYSTEM, SURABAYA

Nova Maulidina Ashuri, Abdul Azis, Noor Nailis Sa'adah 23-26



THE EFFECTS OF WATER FRACTION OF BITTER MELON (MOMORDICA CHARANTIA) LEAF EXTRACT IN MAMMARY GLAND DEVELOPMENT OF BALB/C MICE (MUS MUSCULUS) WITH HISTOLOGICAL AND MOLECULAR BIOLOGICAL ANALYSIS OF PROTEIN APPROACHES

Nur Hayati, Afifah Nur Aini, Nafisatuzzamrudah Nafisatuzzamrudah, Umie Lestari 27-29



COMPETITIVENESS AND POTENTIAL OF SHEEP LIVESTOCK AS SOURCE INCREASING INCOME AND PROVIDER OF MEAT ANIMAL IN NORTH SUMATRA

Sarim Sembiring

30-31



MORPHOLOGICAL AND PHYSIOLOGICAL CHARACTERS OF CASSAVA (MANIHOT ESCULENTA CRANTZ) WHICH WET TOLERANT

Rahmawati Rahmawati, Tri Agus Siswoyo, Didik Puji Restanto, Sri Hartatik, Sigit Soeparjono, Sholeh Avivi 32-35



THE EFFECT OF SOY TEMPEH FLOUR EXTRACT ON VAGINA HISTOLOGICAL STRUCTURE OF SWISS WEBSTER OVARIECTOMIZED MICE (MUS MUSCULUS)

Mahriani Mahriani, Eva Tyas Utami, Dita Ayu Faradila 36-38



THE TOXICITY OF SEEDS EXTRACT OF ANNONA SQUAMOSA L., LEAVES EXTRACT OF TERMINALIA CATAPPA L. AND LEAVES EXTRACT OF ACACIA NILOTICA L. ON THE MORTALITY OF AEDES AEGYPTI L. LARVAE

Dwi Wahyuni, Sandy Pradipta, Muhammad Ramadhan 39-41



ELEPHANTOPUS SCABER AND SAUROPUS ANDROGYNUS REGULATE MACROPHAGES AND B LYMPHOCYTE CELLS DURING SALMONELLA TYPHI INFECTION

Muhammad Sasmito Djati, Dinia Rizqi Dwijayanti, Lulut Dwi Nurmamulyosari, Yayu Fuadah, Muhammad Basyarudin, Nur Jannah

42-44



The Effort To Increase Production of Super Red Dragon Fruit (Hylocereus costaricensis) By Artificial Pollination

Neni Andayani, Lailatun Naria Latifah, Theresia Maria Astuti 45-46



EVALUATION OF ZONATION OF THE MANGROVE CONSERVATION AREAS IN PAMURBAYA

Viv Djanat Prasita, Agus Subianto, Asbar Asbar 47-49



INPUT OF NUTRIENT (NITROGEN AND PHOSPHORUS) FROM THE CATCHMENT AREA INTO RAWAPENING LAKE OF CENTRAL JAVA

Agatha Sih Piranti, Diana RUS Rahayu, Gentur Waluyo 50-51



RELATIONSHIP BETWEEN WATER QUALITY AND ABUNDANCE OF CYANOPHYTA IN PENJALIN RESERVOIR

Badrun Mahera Agung, Agatha Sih Piranti, Carmudi Carmudi 52-56



HEMATOLOGICAL CHARACTERISTIC OF THE FEMALE ASIAN VINE SNAKE (AHAETULLA PRASINA BOIE, 1827)

I Gusti A. Ayu Ratna Puspita Sari, Endah Sri Palupi 57-59



HIGHLY SPESIFIC BACILLUS CEREUS-PHAGES ISOLATED FROM HOSPITAL WASTEWATER IN BANYUMAS REGENCY

Anwar Rovik, Saefuddin 'Aziz, Hendro Pramono 60-64



BIOSYNTHESIS SILVER NANOPARTICLE USING FRESH WATER ALGAE

Dahlia Dahlia, Sherry Aristyani, Robiatul Hadawiyah 65-66



EFFECT OF SAPONIN-PODS EXTRACT ACACIA (ACACIA MANGIUM) TO HEMATOCRIT, HEMOGLOBIN AT TILAPIA (OREOCHROMIS NILOTICUS)

Is Yuniar, Win Darmanto, Agoes Soegianto 67-69



EFFECT OF DISSOLVED NUTRIENT CONCENTRATION (NITRATE AND ORTHOPHOSPHATE) ON ABUNDANCE OF CHLOROPHYTA IN PENJALIN RESERVOIR BREBES REGENCY

Novi Ariyanti, Carmudi Carmudi, Christiani Christiani 70-73



THE ANATOMY OF CAROTENE BIOSYNTHESIS IN BETA VULGARIS L., VAR. RUBRA USING SCAN ELECTRON MICROSCOPE

Dahlia Dahlia 74-76



OPTIMIZATION OF YOGURT FERMENTED MILK PRODUCTS WITH THE ADDITION OF NATURAL STABILIZER BASED ON LOCAL POTENTIAL OF TARO STARCH (COLOCASIA ESCULENTA)

Aju Tjatur Nugroho Krisnaningsih, Dyah Lestari Yulianti, Imam Thohari, Puguh Surjowardojo 77-79



PTERIDOPHYTES OF ALAS PURWO NATIONAL PARK AND THEIR MEDICINAL POTENCY

Fuad Bahrul Ulum, Dwi Setyati

80-82



GENETIC VARIATION OF AEDES AEGYPTI (DIPTERA : CULICIDAE) BASED ON DNA POLYMORPHISM

Rike Oktarianti, Sri Mumpuni

83-84



THE EFFECT OF SOY TEMPEH FLOUR EXTRACT TO UTERINE HISTOLOGY OF OVARIECTOMIZED MICE

Eva Tyas Utami, Mahriani Mahriani, Nidaul Hikmah 85-87



MATING BEHAVIOUR OF CROCIDOLOMIA PAVONANA F.

Purwatiningsih Purwatiningsih, Mirza Devara 88-90

□ PDF

THE DEVELOPMENT OF SUSTAINABLE RESERVE FOOD GARDEN PROGRAM'S VIDEO IN MALANG CITY

Benny Satria Wahyudi, Mimien H. I Al-Muhdhar, Sueb Sueb, Susilowati Susilowati, Endang Budiasih 92-96



EFFECT OF MEDIUM COMPOSITIONS ON THE GROWTH OF RICE (ORYZA SATIVA L. CV. CIHERANG) CALLUS

Ruliana Umar, Yossi Wibisono, Netty Ermawati 97-100



BLOOD FIGURE OF RAMBON CATTLE FED FORMULATED CONCENTRATE CONTAINING SOYBEAN CAKE, POLLARD AND CORN OIL COMBINE WITH UREA XYLANASE MOLASSES CANDY

Emy Koestanti, Romziah S., Tri Bhawono D.

101-102



STRATEGIES FOR DEVELOPMENT OF BEEF CATTLE FARMING BASED ON INNOVATION TECHNOLOGY AND FEEDING PROGRAM TO MEET SELF SUFFICIENCY IN MEAT

Romziah S., Hario P. S., Tri Bhawono D.

103-105



MODIFICATION OF BEAN SPROUT AND UREA MEDIA TO SPIRULINA PLATENSIS CULTURE

Nadya Adharani, Selly Candra Citra, Nova Bagus Hidayat, Agung Hermawan Susanto, Angga Saputra 107-110



COLLAGEN FROM SEA CUCUMBER (STICHOPUS VARIEGATUS) AS AN ALTERNATIVE SOURCE OF HALAL COLLAGEN

M. H. Khirzin, Sukarno Sukarno, N. D. Yuliana, Laily Yunita Susanti, E. Chasanah, Y. N. Fawziya



DEVELOPMENT OF NEW PRODUCT "COCOA SPIRULINA AS FUNCTIONAL FOOD"

Asmak Afriliana, Achmad Subagio, Aminah Abdullah



THE PROTEIN AND WATER CONTENT OF TEN VARIATIONS OF THE FEED CASSAPRO OF YEAST TAPE

Indrawaty Sitepu



EFFECT OF POMELO (CITRUS GRANDIS) ETHANOLIC EXTRACT ON ATHEROSCLEROTIC PLAQUE FORMATION

Mudzakkir Taufiqurrahman, Kiky Martha Ariesaka, Hilda Khairinnisa, Wahyu Dian Puspita, Azka Darajat, Al Munawir



CLINICAL MANIFESTATION OF ORAL TUBERCULOSIS

Atik Kurniawati, Ni Made Mertaniasih, Mangestuti Agil



IDENTIFICATION OF DERMATOPHYTES BY MULTIPLEX-POLYMERASE CHAIN REACTION, POLYMERASE CHAIN REACTION-RESTRICTION FRAGMENT LENGTH POLYMORPHISM ITSI-ITS4 PRIMERS AND MVAI, AND POLYMERASE CHAIN REACTION (GACA)4 PRIMER

Rizalinda Sjahril, Firdaus Hamid, Aan Yulianingsih, Novita Prastiwi, Awaluddin Awaluddin, Siska Nuryanti, Faridha Ilyas, Burhanuddin Bahar 132-135



[RETRACTED] IMPACT PSYCHOLOGICAL AND PSYCHO-PHYSICAL WORK DISTRESS ON TOOTH MOBILITY IN RAT MODEL (ARTICLE RETRACTED FROM IBSC PROCEEDING)

Zahreni Hamzah, Suhartono Taat Putra, Elyana Asnar STP 136-139

ROLE OF REACTIVE OXYGEN SPECIES ON DEVELOPMENTS OF OSTEOCLASTOGENESIS IN AGING

Dyah Indartin Setyowati, Zahreni Hamzah, Zahara Meilawaty 140-143



DETERMINANT FACTOR THAT INFLUENCED ANXIETY LEVEL AND ENERGY INTAKE AMONG ELDERLY

Ninna Rohmawati



P-CARE BPJS ACCEPTANCE MODEL IN PRIMARY HEALTH CENTERS

Hosizah Hosizah



THE EFFORT OF TB CADRE IN THE IMPROVING OF THE SUCCESS OF TB THERAPY AND REDUCING SIDE EFFECTS OF ANTI TUBERCULOSIS DRUGS

Dewi Rokhmah, Khoiron Khoiron, Elly Nurus Shakinah, Ema Rahmawati 151-152



RISK FACTOR OF GREEN TOBACCO SICKNESS (GTS) AT THE CHILDREN ON TOBACCO PLANTATION

Dewi Rokhmah, Khoiron Khoiron

153-156



DIRECT SCATTERING PROBLEM FOR MICROWAVE TOMOGRAPHY

Agung Tjahjo Nugroho

158-161



MICROSTRUCTURE AND MECHANICAL PROPERTIES OF DISSIMILAR JOINT OF COLD ROLLED STEEL SHEETS 1.8 SPCC-SD AND NUT WELD M6 BY SPOT WELDING

Ratna Kartikasari, Mustakim Mustakim, Joko Pitoyo, Feri Frandika 162-164



FEATURE EXTRACTION OF HEART SIGNALS USING FAST FOURIER TRANSFORM

Hindarto Hindarto, Izza Anshory, Ade Efiyan

165-167



ANALYSIS OF EL NIÑO EVENT IN 2015 AND THE IMPACT TO THE INCREASE OF HOTSPOTS IN SUMATERA AND KALIMANTAN REGION OF INDONESIA

Ardila Yananto, Saraswati Dewi 168-173



SYNTHESIS OF ZINC OXIDE (ZNO) NANOPARTICLE BY MECHANO-CHEMICAL METHOD

Siswanto Siswanto, Anita Yuliati, Mayasari Hariyanto



MODELLING DYNAMICS OF ZNO PARTICLES IN THE SPRAY PYROLISIS REACTOR TUBE

Diky Anggoro, Melania Muntini, Iim Fatimah, Sudarsono Sudarsono 177-180



THE INFLUENCE OF EXTREMELY LOW FREQUENCY (ELF) MAGNETIC FIELD EXPOSURE ON THE PROCESS OF MAKING CREAM CHEESE

Andika Kristinawati, Sudarti Sudarti 181-183



Au Grade of Epithermal Gold Ore at Paningkaban ASGM, Banyumas District, Central Java Province, Indonesia

Rika Ernawati, Arifudin Idrus, HTBM Petrus 184-187



Renewable Energy Conversion with hybrid Solar Cell and Fuel Cell

Aris Ansori, Indra Herlamba Siregar, Subuh Isnur Haryuda



Radar Absorbing Materials Double Layer From Laterite Iron Rocks And Actived Carbon Of Cassava Peel In X-Band Frequency Range

Linda Silvia, Bayu Aslama, Ega Novialent, M. Zainuri 192-194



Instantaneous Analysis Attribute for Reservoir Characterization at Basin Nova-Scotia, Canada

Ruliyanti Ruliyanti, Puguh Hiskiawan, Artoto Arkundato 195-196



Deployment Porosity Estimation of Sandstone Reservoir in The Field of Hidrocarbon Exploration Penobscot Canada

Himmah Khasanah, Puguh Hiskiawan, Supriyadi Supriyadi 197-198



Seismic Resolution Enhacement with Spectral Decomposition Attribute at Exploration Field in Canada

Illavi Praseti Pebrian, Puguh Hiskiawan, Artoto Arkundato 199-203



Simulation of I-V Characteristics of Si Diode at Difference Operating Temperature:Effect of Ionized Impurity Scattering

Siti Lailatul Arofah, Endhah Purwandari, Edy Supriyanto 204-206



Simulatian of self diffusion of iron (Fe) and Chromium (Cr) in Liquid lead by Molecular Dynamic

Ernik Dwi S, Artoto Arkundato, Supriyadi Supriyadi, Heru Baskoro, Elva Nurul F 207-208



The Study of Electrical Conductance Spectroscopy of The Inner membrane of Salak

Wenny Maulina

209-210



The Accuracy Comparison of Oscilloscope and Voltmeter Utilizated in Getting Dielectric Constant Values

Bowo Eko Cahyono, Misto Misto, Rofiatun Rofiatun 211-213



Window Filter (WinTer) To Capture Pollution of Lead (Pb) For Houses Near The Highway To Prevent Health Problems

Rifang Pri Asmara, Fitri Azizah, Siti Umi Afifah

214-215



Simulation of Solar Cell Diode I-V Characteristics Using Finite Element Methode: Influence of p- Layer Thickness

Greta Andika Fatma, Endhah Purwandari, Edy Supriyanto 216-217



GIS-based optimization method for utilizing coal remaining resources and post-mining land use planning: A case study of PT Adaro coal mine in South Kalimantan

Mohamad Anis, Arifudin Idrus, Hendra Amijaya, Subagyo Subagyo 219-225



Quantification Model of Qualitative Geological Data Variables for Exploration Risk Assessment in Prospect Cu-Au Porphyry Deposit Randu Kuning, Wonogiri, Central Java

Nurkhamim Nurkhamim, Arifudin Idrus, Agung Harijoko, Irwan Endrayanto, Sapto Putranto 226-23



A Sensor-Based of Detection Tools To Mitigate People Live in Areas Prone to Landslide

Satryo Budi Utomo, Januar Fery Irawan

232-236



Relocation of hypocenter using Jacobian's matrix and Jeffreys-Bullen's velocity model

Faid Muhlis, Risca Listyaningrum, Indriati Retno Palupi 237-238



Analysis Of The Geothermal Potential Based Fault Zone In Burni Telong Bener Meriah, Aceh, Indonesia

Gartika Setiya Nugraha, Marwan Marwan, Oky Ikhramullah, Susanti Alawiyah, Sutopo Sutopo 239-242



Synthesis Of Zeolites From Lombok Pumice As Silica Source For Ion Exchanger

Mega Putri K., Regina G.L. D., Ade L.N. F., Haiyina H. A., Nura H. H., Darminto Darminto 244-247



Optimisation of Extractant and Extraction Time on Portable Extractor Potentiometric Method for Determining Phosphate in Soil

Anggia Rose Sukaton, Siswoyo Siswoyo, Bambang Piluharto 248-252



Analysis of protein profile of neem leaves juice (azadirachta indica I. Juss)

I Dewa Ayu Ratna Dewanti, I Dewa Ayu Susilawati, Pujiana Endah Lestari, Roedy Budirahardjo 253-255



Hydrophobic Aerogel-Based Film Coating On Glass By Using Microwave

Poerwadi Bambang, Diah Agustina P, Christia Meidiana 256-258



Preparation and Characterization of Cacao Waste As Cacao Vinegar And Charcoal

Mohammad Wijaya, Muhammad Wiharto 259-261



The Effect of Physico-Chemical Properties of Aquatic sediment to the Distribution of Geochemical Fractions of Heavy Metals in the Sediment

Barlah Rumhayati, Catur Retnaningdyah, Novi Anitra, Ahmad Dodi Setiadi 262-265



Increased Concentration of Bioethanol by Rectification Distillation Sieve Tray Type

Yuana Susmiati, Mochamad Nuruddin

266-269



Determination of Lead in Cosmetic Sampels Using Coated Wire Lead (II) Ion Selective Electrode Based On Phyropillite

Qonitah Fardiyah, Barlah Rumhayati, Ika Rosemiyani 270-272



Pyrolysis Temperature Effect on Volume and Chemical Composition of Liquid Volatile Matter of Durian Shell

Waode O.S. Ilmawati, M. Jahiding, Waode O.S. Musnina 273-275



High Performance Liquid Chromatography of Amino Acids Using Potentiometric Detector With A Tungsten Oxide Electrode

Yeni Maulidah Muflihah, Zulfikar Zulfikar, Siswoyo Siswoyo, Asnawati Asnawati, Qurrota Ayun 276-278



Rainwater Treatment Using Treated Natural Zeolite and Activated Carbon Filter

Lili Mulyatna, Yonik M. Yustiani, Astri Hasbiah, Widya Yopita 279-281



Filtration of Protein in Tempe Wastewater Using Cellulose Acetate Membrane

Dwi Indarti, Badrut Tamam Ibnu Ali, Tri Mulyono 282-284



Image Encryption Technique Based on Pixel Exchange and XOR Operation

Kiswara A. Santoso, Fatmawati Fatmawati, Herry Suprajitno 286-288



Fuzzy Anp Method And Internal Business Perspective For Performance Measurement In Determining Strategy SMEs

Yeni Kustiyahningsih, Eza Rahmanita, Jaka Purnama 289-294



Application of Fuzzy TOPSIS Method in Scholarship Interview

Abduh Riski, Ahmad Kamsyakawuni

295-298



The Effect of Inflation, Interest Rate, and Indonesia Composite Index (ICI) to the Performances of Mutual Fund Return and Unit Link with Panel Data Regression Modelling

Siti S. Purwaningsih, Anny Suryani, Euis Sartika 299-302



Using Logistic Regression to Estimate the Influence of Adolescent Sexual Behavior Factors on Students of Senior High School 1 Sangatta, East Kutai-East Kalimantan

Darnah Darnah, Memi Norhayati

303-306



Application Cluster Analysis on Time Series Modelling with Spatial Correlations for Rainfall Data in Jember Regency

Ira Yudistira, Alfian Futuhul Hadi, Dian Anggraeni, Budi Lestari 307-310



A Zero Crossing-Virus Evolutionary Genetic Algorithm (VEGA) to Solve Nonlinear Equations

M. Ziaul Arif, Zainul Anwar, Ahmad Kamsyakawuni 311-315



Analysis of Simultaneous Equation Model (SEM) on Non normally Response used the Method of Reduce Rank Vector Generalized Linear Models (RR-VGLM)

Miftahul Ulum, Alfian Futuhul Hadi, Dian Anggraeni 316-318



The Rainbow (1,2)-Connection Number of Exponential Graph and It's Lower Bound

Gembong A. W., Dafik Dafik, Ika Hesti Agustin, Slamin Slamin 319-320



Construction of Super H-Antimagicness of Graph by Uses a Partition Technique with Cancelation Number

Rafiantika Megahnia Prihandini, Dafik Dafik, Ika Hesti Agustin 321-324



On The Total r-dynamic Coloring of Edge Comb Product graph G D H

Dwi Agustin Retno Wardani, Dafik Dafik, Antonius C. Prihandoko, Arika I. Kristiana 325-327



On The Metric Dimension with Non-isolated Resolving Number of Some Exponential Graph

S. M. Yunika, Slamin Slamin, Dafik Dafik, Kusbudiono Kusbudiono 328-330



On Total r-Dynamic Coloring of Several Classes of Graphs and Their Related Operations

Kusbudiono Kusbudiono, Desi Febriani Putri, Dafik Dafik, Arika Indah Kristiana 331-336



The Analysis of r-dynamic Vertex Colouring on Graph Operation Of Shackle

Novita Sana Susanti, Dafik Dafik

337-339



On the Rainbow Vertex Connection Number of Edge Comb of Some Graph

Agustina M., Dafik Dafik, Slamin Slamin, Kusbudiono Kusbudiono 340-342



On the edge r-dynamic chromatic number of some related graph operations

Novian Nur Fatihah, Arika Indah Kriatiana, Ika Hesti Agustin, Dafik Dafik 343-346



Handling Outlier In The Two Ways Table By Using Robust Ammi And Robust Factor

Kurnia Ahadiyah, Alfian Futuhul Hadi, Dian Anggraeni 347-350



An Epidemic Model of Varicella with Vaccination

Qurrota A'yuni Ar Ruhimat, Imam Solekhudin 351-355



The Correlation Between Perception And Behavior Of River Pollution By Communities Around Brantas Riverbank In Malang

Kuni Mawaddah, Sueb Sueb 357-359



Isolation And Screening Of Specific Methicillin Resistant-Staphylococcus Aureus Bacteriophage From Hosiptal Waste At Banyumas

Chairunisa Fadhilah, Saefuddin Aziz, Hendro Pramono 360-364



Co(III) as Mediator in Phenol Destruction Using Electrochemical Oxidant

Herlina Herlina, Derlini Derlini, Muhammad Razali





Design of System Batch Injection Analysis (BIA) for Monitoring the Production of Alcohol (II)

Tri Mulyono, Dwi Indarti, Rizqon Rizqon 370-374



Preliminary Study Gold Mineralization Hosted By Metamorphic Rocks In The Southeastern Arm Of Sulawesi, Indonesia

Hasria Hasria, Arifudin Idrus, I Wayan Warmada 375-378



Effects of Packaging Types on Moisture Content, Microbe Total and Peroxide Value of Instant Ganyong (Canna edulis Kerr) Yellow Rice

Lilis Sulandari

379-383



Resistivity Value as Characteristics Of Majapahit Kingdom Era Red Bricks

Supriyadi Supriyadi, Nurul Priyantari, Rosaria Dwi Sukmadewi 384-385



Strategy to Increase Contract Farming Satisfaction on Red Chili Farmer with The Hortikultura Lestari Cooperation (Evidence: Dukuh Dempok Village Wuluhan District)

Hesti Herminingsih





On Total r-Dynamic Coloring of Several Classes of Graphs and Their Related Operations

Kusbudiono^{1,3}, Desi Febriani Putri³, Dafik^{1,2}, Arika Indah Kristiana^{1,2}

¹CGANT University of Jember Indonesia

²Mathematics Edu. Depart. University of Jember Indonesia

³Mathematics Depart. University of Jember Indonesia

e-mail: kusbudiono@unej.ac.id

Abstract—All graphs in this paper are simple, connected and undirected. Let r,k be natural numbers. By a proper k-coloring of a graph G, we mean a map $c:V(G)\to S$, where |S|=k, such that any two adjacent vertices receive different colors. A total r-dynamic coloring is a proper k-coloring c of G, such that $\forall v\in V(G), |c(N(v))|\geq \min[r,d(v)+|N(v)|]$ and $\forall uv\in E(G), |c(N(uv))|\geq \min[r,d(u)+d(v)]$. The total r-dynamic chromatic number, written as $\chi''_r(G)$, is the minimum k such that G has an r-dynamic k-coloring. Finding the total r-dynamic chromatic number is considered to be a NP-Hard problems for any graph. Thus, in this paper, we initiate to study $\chi''_r(G)$ of several classes of graphs and and their related operations.

Keywords—Total *r*-Dynamic Chromatic Number, Several Slasses of Graphs, Graph Operations.

INTRODUCTION

Graph G is a couple of (V(G), E(G)) with V(G) is finite set not empty of elements called vertex, and E(G) is a set (maybe empty) of a pair not ordered (u,v) called edge [1]. A graph G possible not having edge, but must be having vertex at least one. A graph who do not have edges but having a vertex only called by trivial graph. [2]. The number of vertices on a graph called vertex cardinality and denoted by |V| while the number of edges on a graph called edge cardinality with denoted by |E| [3].

One study in graph theory is graph coloring. Graph coloring be a function that maps elements elements to any set of. If the domain set was a edge called edge coloring. If the domain set was vertex hence called vertex coloring. If the domain set vertex and edge called total coloring. Total coloring is a function c that maps (V(G), E(G)) to the set of color so much for any two vertices neighbors, and every two edges neighbors and any vertex of which is one side with random edge has of different colors. Minimum number of colors called to the chromatic number, and always based alleged 1 as follows:

Conjecture 1 According to behzad and vizing the chromatic number of total for each graph G must satisfy $\Delta(G) + 1 \leq \chi''(G) \leq \Delta(G) + 2$ [4]

One study in graph theory is a total r-dynamic coloring developed from the vertex and edge r-dynamic coloring. Total coloring k-color r-dynamic is total coloring for every $v\in V(G)$ so $|c(N(v))|\geq min[r,d(v)+|N(v)|],$ and every edge $e=uv\in E(G)$ so much $|c(N(e))|\geq min[r,d(v)+d(u)]$ where N(v) is neighbor v dan c(N(v)) is color that used by vertex neighbors v and N(e) is neighbors edge e and c(N(e)) is color that used by edge neighbors edge e. Minimum number k so graph G satisfy total coloring k-color r-dynamic called chromatic number total r-dynamic denoted by $\chi''(G)$. The following are several definition operation graph used in this article.

Definition 1. Shackle graph H denoted by G = shack(H,v,n) is graph G generate of non trivial graph $H_1,H_2,...,H_n$ so for all $1 \leq s,t \leq n$, H_s and H_t not having a vertex liaison where $|s-t| \geq 2$ and for all $1 \leq i \leq n-1$, H_i and H_{i+1} have exactly one vertex fellowship v, called with a vertex liaison and k-1 connecting the vertex was different. If G = shack(H,v,n) liaison vertex replaced by subgraph $K \subset H$ called by generalized shackle, dan denoted by $G = gshack(H,K \subset H,n)$

THE RESULTS

The results from the study is the definition and a new theorem related a total r-dynamic coloring. Definition of total r-dynamic coloring can be seen in definition 2.

The theorem about a total r-dynamic coloring on graph of path, shackle book graph $(shack(B_2,v,n)$ dan graph operation generalized shackle graph friendship $gshack(\mathbf{F}_4,e,n)$.

Definition 2. Let $D = \{1, 2, 3, \dots, k\}$ is set of color by k colors dan c is function maps all vertices and edges G to set of colors. Total r-dynamic coloring of graph G is defined as mapping c from $(V(G) \cup E(G))$ to D so satisfy a condition the following :

1.
$$\forall v \in V(G)$$
, $|c(N(v))| \ge min[r, d(v) + |N(v)|]$ dan

2.
$$\forall e = uv \in E(G), |c(N(e))| \ge min[r, d(v) + d(u)]$$

Observation 1. Let $\Delta(G)$ is maximum degree of graph G so $\chi''(G) \leq \chi''_d(G) \leq \chi''_3(G) \leq \cdots \leq \chi''_{\Delta(G)}(G)$.

 \Diamond **Theorem 1.** Let G is a path P_n . For $n \geq 3$, chromatic number total r-dynamic of graph G is

$$\chi_r''(P_n) = \begin{cases} 3, \text{ for } 1 \le r \le 2\\ 4, \text{ for } r = 3 \end{cases}$$

5, for
$$r \geq 4$$

Proof. Set of vertices and set of edges of path for $n \geq 3$ is $V(P_n) = \{x_i; 1 \leq i \leq n\}$ and $E(P_n) = \{x_ix_{i+1}; 1 \leq i \leq n-1\}$, so $|V(P_n)| = n$ and $|E(P_n)| = n-1$ and $\Delta(G) = 2$.

Case 1. Based on Conjecture 1 that $\Delta(G)+1 \leq \chi_n''(G) \leq \Delta(G)+2$, so $\chi''(P_n) \geq 3$. To prove that chromatic number of total 1, 2-dynamic coloring of path (P_n) is 3, needs to be proven $\chi''(P_n) \geq 3$ and $\chi''P_n) \leq 3$. Then indicated that the number of chromatic $\chi''(P_n) \leq 3$ to coloring function c_1 . Let $D=\{1,2,3,\ldots,k\}$ is set of colors by k colors

$$c_1(x_1,x_2,\dots,x_i) = \begin{cases} & 132\dots132,\\ & 1\leq i\leq n,\\ & i\equiv 0 (\text{mod } 3) \end{cases}$$

$$c_1(x_1,x_2,\dots,x_i) = \begin{cases} & 132\dots132\ 1,\\ & 1\leq i\leq n,\\ & i\equiv 1 (\text{mod } 3) \end{cases}$$

$$\vdots$$

$$132\dots132\ 13,$$

$$1\leq i\leq n,$$

$$1\leq i\leq n,$$

$$1\leq i\equiv 2 (\text{mod } 3)$$



$$c_1(x_1x_2,\dots x_ix_{i+1}) = \begin{cases} 213\dots 213, \\ 1\leq i\leq n, \\ i\equiv 0 (\text{mod } 3) \end{cases}$$

$$c_1(x_1x_2,\dots x_ix_{i+1}) = \begin{cases} 213\dots 213 \ 2, \\ 1\leq i\leq n, \\ i\equiv 1 (\text{mod } 3) \end{cases}$$

$$213\dots 213 \ 21, \\ 1\leq i\leq n, \\ i\equiv 2 (\text{mod } 3) \end{cases}$$

From coloring function of c_1 it can be seen that the number of chromatic total in graph the is $\chi''(P_n) \leq 3$. Since $\chi''(P_n) \leq 3$ and $\chi''(P_n) \geq 3$ than $\chi''(P_n) = 3$, for $n \geq 3$.

Case 2. Base of Observation 1 that $\chi_3''(G) \geq \chi_2''(G)$, then $\chi_3''(P_n) \geq \chi_d''(P_n) = 3$. Let $\chi_3''(P_n) = 3$ as on coloring function c_1 , So does not meet the definition of the total r-dynamic coloring. Leading to the need for additional colors become 4-coloring, $\chi_3''(P_n) \geq 4$.

To proven chromatic number of total 3-dynamic coloring of path (P_n) is 4, needs to be proven $\chi_3''(P_n) \geq 4$ and $\chi_3''(P_n) \leq 4$. Then indicated that the number of chromatic $\chi_3''(P_n) \leq 4$ by coloring function c_2 . Let $D = \{1, 2, 3, \ldots, k\}$ is set of colors by k color and c_2 is function who pairs every vertic es and edges to set D, $c_2: (V(P_n) \cup E(P_n)) \to D$. For $n \geq 3$, coloring function c_2 is as follows:

$$c_2(x_1, x_2, \dots, x_i) = \begin{cases} & 13 \dots 13, \\ & 1 \le i \le n, \\ & n \text{ even} \end{cases}$$

$$c_2(x_1, x_2, \dots, x_i) = \begin{cases} & 13 \dots 13, \\ & 1 \le i \le n, \\ & n \text{ odd} \end{cases}$$

$$\begin{cases} & 24 \dots 24, \\ & 1 \le i \le n, \\ & n \text{ even} \end{cases}$$

$$c_2(x_1x_2, \dots x_ix_{i+1}) = \begin{cases} & 24 \dots 24, \\ & 1 \le i \le n, \\ & n \text{ odd} \end{cases}$$

From c_2 it can be seen that the number of chromatic total 3-dynamic is $\chi_3''(P_n) \leq 4$. Since $\chi_3''(P_n) \leq 4$ and $\chi_3''(P_n) \geq 4$ than $\chi_3''(P_n) = 4$ so $\chi_3''(P_n) = 4$ for $n \geq 3$. as illustration, served figure 2 that is the total 3-dynamic coloring of path (P_n) .



Fig 1. Total 3-Dynamic Coloring of Path (P_n)

Case 3. Based on Observation 1 that $\chi_4''(G) \geq \chi_3''(G)$, than $\chi_4''(P_n) \geq \chi_3''(P_n) = 4$. Let $\chi_3''(P_n) = 4$ as on coloring function c_2 , so does no satisfy definition of total r-dynamic coloring. So that required the addition of colors become 5-coloring, $\chi_4''(P_n) \geq 5$.

To prove the chromatic number from the total 4-dynamic coloring of path (P_n) is 5, needs to be proven $\chi_4''(P_n) \geq 5$ and $\chi_4''(P_n) \leq 5$. Then indicated that the chromatic number $\chi_4''(P_n) \leq 5$ by coloring function c_3 . Let $D = \{1, 2, 3, \ldots, k\}$ is set of colors with k colors and c_3 is function pairing any vertex and edge to the set of color $D, c_3: (V(P_n) \cup E(P_n)) \to D$. For $n \geq 3$, coloring function c_3 is as follows:

```
13524...13524,
                                1 \le i \le n,
                                i \equiv 0 \pmod{3}
                                13524 \dots 13524 1.
                                1 \le i \le n,
                                i \equiv 1 (\text{mod } 3)
                                13524 . . . 13524 13.
c_3(x_1, x_2, \dots, x_i) =
                                1 \le i \le n,
                                i \equiv 2 \pmod{3}
                                13524 \dots 13524 \ 135,
                                1 \leq i \leq n,
                                i \equiv 3 \pmod{3}
                                13524 \dots 13524 \ 1352,
                                1 \le i \le n,
                                i \equiv 4 \pmod{3}
                                   24135...
                                      24135,
                                       1 \le i \le n,
                                       i\equiv 1 ({\rm mod}\ 3)
                                       24135\dots
                                      24135 2,
                                       1 \le i \le n,
                                       i \equiv 2 \pmod{3}
                                       24135\dots
  c_3(x_1x_2,\ldots,x_ix_{i+1}) =
                                      1 \le i \le n,
                                       i \equiv 3 \pmod{3}
                                       24135...
                                      24135 241,
                                       1 \le i \le n,
                                       i \equiv 4 \pmod{3}
                                       24135\dots
                                      24135 2413,
                                       1 \le i \le n,
                                       i \equiv 0 \pmod{3}
```

Of coloring function on c_3 It is evident that the chromatic number of total 4-dynamic coloring is $\chi_4''(P_n) \leq 5$. Since $\chi_4''(P_n) \leq 5$ and $\chi_4''(P_n) \geq 5$. So can be concluded $\chi_4''(P_n) = 5$. So chromatic number total $\chi_4''(P_n) = 5$.

On path P_n , If reviewed from the vertices, number of $\min\{r, \max\{d(x_1) + |(N(x_i))|\}\} = \max\{d(x_1) + |(N(x_i))|\} = 4$. If in terms of coloring the edge of on path P_n , number of $\min\{r, \max\{d(u) + d(v)\}\} = \max\{d(u) + d(v)\} = 4$. Resulting in $\chi''_{r\geq 4}(P_n) = 5$. As illustration, served Figure 2 which is 4-dynamic coloring of path (P_n) . Based on the description above, then Theorem \prod proved.

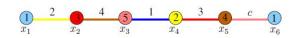


Fig 2. Total r-Dynamic Coloring of Path (P_n)

 \Diamond **Theorem 2.** Let graph G is operation graph shackle of book graph B_2 . For $n \geq 2$, chromatic number of total r-dynamic shackle of book graph $Shack(B_2, v, n)$ is



$$\chi''_r(Shack(B_2, v, n)) = \begin{cases} 5, \text{ for } 1 \le r \le 3\\ 6, \text{ for } r = 4\\ 9, \text{ for } r = 5\\ 10, \text{ for } r \ge 6 \end{cases}$$

Proof. Set of vertices of graph $V(Shack(B_2, v, n)) = \{x_{ij}, z_{ij}; 1 \le i \le n, 1 \le j \le 2\} \cup \{y_i; 1 \le i \le n+1\}$ and set of edges $E(B_2, v, n)) = \{x_{ij}y_i; 1 \le i \le n, j = 1\} \cup \{x_{ij}y_{i+1}; 1 \le i \le n, j = 2\} \cup \{x_{ij}z_{ij+1}; 1 \le i \le n, j = 2\} \cup \{x_{ij}z_{ij+1}; 1 \le i \le n, j = 1\} \cup \{y_{i}z_{ij}; 1 \le i \le n, j = 1\} \cup \{y_{i}z_{ij}; 1 \le i \le n, j = 1\} \cup \{y_{i+1}z_{ij}; 1 \le i \le n, j = 2\} \cup \{z_{ij}z_{ij+1}; 1 \le i \le n, j = 1\}$ so cardinality vertex and edges is $|V(Shack(B_2, v, n))| = 5n + 1$ and $|E(Shack(B_2, v, n))| = 7n$ and $\Delta(G) = 4$.

Case 1. Based on Conjecture 1 that $\Delta(G)+1\leq \chi_r''(G)\leq \Delta(G)+2$, so $\chi''(Shack(B_2,v,n))\geq 5$. To prove the chromatic number total 1,2,3-dynamic coloring of graph $(Shack(B_2,v,n))$ is 5, needs to be proven $\chi''(Shack(B_2,v,n))\geq 5$ and $\chi''(Shack(B_2,v,n))\leq 5$. Then indicated that the chromatic number $\chi''(Shack(B_2,v,n))\leq 5$ by coloring function c_4 . Let $D=\{1,2,3,\ldots,k\}$ is the set of color with k colors and c_4 is function who pairing every vertex and edge to The set of color $D,\ c_4:\ (V(Shack(B_2,v,n))\cup E(Shack(B_2,v,n)))\to D$. Coloring function c_4 is as follows:

$$c_4(x_{ij}) = \begin{cases} 4, & 1 \le i \le n, \ j = 1 \\ 5, & 1 \le i \le n, \ j = 2 \end{cases}$$

$$c_4(z_{ij}) = \begin{cases} 3, & 1 \le i \le n, \ j = 1 \\ 2, & 1 \le i \le n, \ j = 2 \end{cases}$$

$$c_4(y_i) = 1, 1 \le i \le n+1;$$

$$c_{23}(x_{ij}y_i) = 3, 1 \le i \le n, j = 1$$

$$c_4(x_{ij}y_{i+1}) = 3, 1 \le i \le n, j = 2;$$

$$c_4(y_iz_{ij}) = 5, 1 \le i \le n, j = 1$$

$$c_4(y_{i+1}z_{ij}) = 4, 1 \le i \le n, j = 2;$$

$$c_4(x_{ij}z_{ij+1}) = 2, 1 \le i \le n, j = 1$$

$$c_4(x_{ij}z_{ij+1}) = 3, 1 \le i \le n, j = 1;$$

$$c_4(z_{ij}z_{ij+1}) = 1, 1 \le i \le n, j = 1$$

Of coloring function on c_4 It is evident that the chromatic number Total ofshackle book graph $(Shack(B_2,v,n))$ is $\chi''(Shack(B_2,v,n)) \leq 5$. Since chromatic number $\chi''(Shack(B_2,v,n))$

 $\leq 5 \text{ and } \\ \chi''(Shack(B_2,v,n)) \geq 5 \text{ So it can be concluded } \\ \chi''(Shack(B_2,v,n)) = 5. \text{ So that graph } G = \\ Shack(B_2,v,n) \text{ have chromatic numbers } \chi''(G) = \\ \chi''_d(G) = \chi''_3(G) = 5.$

Case 2. Based on Observation 1 that $\chi_4''(G) \ge \chi_3''(G)$, Can be concluded $\chi_4''(Shack(B_2, v, n)) \ge \chi_3''(Shack(B_2, v, n))$. Let $\chi_4''(Shack(B_2, v, n)) = 5$ As on coloring function c_4 , So does not meet the definition total r-dynamic coloring. So that required the addition of color be 6-coloring, $\chi_4''(Shack(B_2, v, n)) \ge 6$.

To prove the chromatic number from the total 4-dynamic on graph $(Shack(B_2,v,n))$ is 6, need to be proven that $\chi_4''(Shack(B_2,v,n)) \geq 6$ and $\chi_4''(Shack(B_2,v,n)) \leq 6$. Then indicated that the chromatic number $\chi_4''(Shack(B_2,v,n)) \leq 6$ by coloring function c_5 . Let $D=\{1,2,3,\ldots,k\}$ is the set of color with k colors and c_5 is function who pairing every vertex and edges to set of colors $D, c_5: V(Shack(B_2,v,n)) \cup E(Shack(B_2,v,n)) \rightarrow D$. Coloring function c_5 is as

follows:

$$c_5(x_{ij}) = \begin{cases} 6, \ 1 \le i \le n, \ j = 1\\ 3, \ 1 \le i \le n, \ j = 2 \end{cases}$$
$$c_5(z_{ij}) = \begin{cases} 4, \ 1 \le i \le n, \ j = 1\\ 5, \ 1 \le i \le n, \ j = 2 \end{cases}$$

$$c_5(y_i) = 1, 1 \le i \le n+1;$$
 (1)

$$c_{24}(x_{ij}y_i) = 2, 1 \le i \le n, j = 1 \tag{2}$$

$$c_5(x_{ij}y_{i+1}) = 6, 1 \le i \le n, j = 2;$$
 (3)

$$c_5(y_i z_{ij}) = 5, 1 \le i \le n, j = 1$$
 (4)

$$c_5(y_{i+1}z_{ij}) = 4, 1 \le i \le n, j = 2;$$
 (5)

$$c_5(x_{ij}z_{ij+1}) = 3, 1 \le i \le n, j = 1$$
 (6)

$$c_5(x_{ij+1}z_{ij}) = 2, 1 \le i \le n, j = 1;$$
 (7)

$$c_5(z_{ij}z_{ij+1}) = 6, 1 \le i \le n, j = 1 \tag{8}$$

Of coloring function on c_5 It is evident that the chromatic number total of *shackle* book graph, $G=(Shack(B_2,v,n))$ is $\chi_4''(G)\leq 6$. Since $\chi_4''(G)\leq 6$ dan $\chi_4''(G)\geq 6$ then $\chi_4''(G)=6$ so chromatic number $\chi_4''(G)=6$. As illustration, served Picture 4.24 Which is coloring 4-dynamic of *shackle* book graph B_2 .

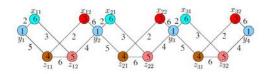


Fig 3. Total 4-dynamic Coloring of Book Graph $Shack(B_2, v, n)$

Case 3. Based on Observation that $\chi_5''(G) \geq \chi_4''(G)$, Can be concluded $\chi_5''(Shack(B_2,v,n)) \geq \chi_5''(Shack(B_2,v,n))$. Let $\chi_5''(Shack(B_2,v,n)) = 6$ As on coloring function c_5 , So does not meet definition of total r-dynamic coloring so that required the addition of colors become 7-coloring, then $\chi_5''(Shack(B_2,v,n)) \geq 7$. But with 7 coloring still not meet Total 5-dynamic coloring So that plus to 8 coloring. For 8 coloring there are the number of edge that do not meet the definition of total r-dynamic coloring so plus to 9 coloring so $\chi_5''(Shack(B_2,v,n)) \geq 9$.

To prove chromatic numbers of the total 5-dynamic coloring on graph $Shack(B_2,v,n)$ is 9, needs to be proven $\chi_5''(Shack(B_2,v,n)) \geq 9$ and $\chi_5''(Shack(B_2,v,n)) \leq 9$. Then indicated that the chromatic number $\chi_5''(Shack(B_2,v,n)) \leq 9$ by coloring function c_6 . Let $D=\{1,2,3,\ldots,k\}$ is set of colors with k colors and c_6 is function who pairing every vertex and edges to set of color $D, c_6: (V(Shack(B_2,v,n)) \cup E(Shack(B_2,v,n))) \rightarrow D$. For $n \geq 2$, coloring function c_6 Is as follows:

$$c_6(x_{ij}) = \begin{cases} 4, & 1 \le i \le n, \ j = 1\\ 3, & 1 \le i \le n, \ j = 2 \end{cases}$$
$$c_6(z_{ij}) = \begin{cases} 6, & 1 \le i \le n, \ j = 1\\ 2, & 1 \le i \le n, \ j = 2 \end{cases}$$

 $\begin{array}{c} c_6(y_i) = 1, 1 \leq i \leq n+1; c_6(x_{ij}y_i) = 8, 1 \leq i \leq \\ n, j = 1c_6(x_{ij}y_{i+1}) = 9, 1 \leq i \leq n, j = 2; \quad c_6(y_iz_{ij}) = \\ 2, 1 \leq i \leq n, j = 1c_6(y_{i+1}z_{ij}) = 5, 1 \leq i \leq n, j = 2; \quad c_6(x_{ij}z_{ij+1}) = 3, 1 \leq i \leq n, j = 1c_6(x_{ij+1}z_{ij}) = \\ 4, 1 \leq i \leq n, j = 1; \quad c_6(z_{ij}z_{ij+1}) = 7, 1 \leq i \leq n, j = 1 \end{array}$

Of coloring function on c_6 It is evident that the chromatic number total of *shackle* book graph, $G=(Shack(B_2,v,n))$ is $\chi_5''(G)\leq 9$. Since $\chi_5''(G)\leq 9$ and $\chi_5''(G)\geq 9$ then $\chi_5''(G)=9$ so chromatic number $\chi_5''(G)=9$.



Case 4. Based on Observation that $\chi_6''(G) \geq \chi_5''(G)$, Can be concluded $\chi_6''(Shack(B_2,v,n)) \geq \chi_5''(Shack(B_2,v,n))$. Let $\chi_5''(Shack(B_2,v,n)) = 9$ As on coloring function c_6 , So does not meet definition of total r-dynamic coloring so that required the addition of colors become 10-coloring, then $\chi_6''(Shack(B_2,v,n)) \geq 10$.

To prove chromatic numbers of the total 6-dynamic coloring on graph $Shack(B_2,v,n)$ is 10, needs to be proven $\chi_6''(Shack(B_2,v,n)) \geq 10$ and $\chi_6''(Shack(B_2,v,n)) \leq 10$. Then indicated that the chromatic number $\chi_6''(Shack(B_2,v,n)) \leq 10$ by coloring function c_7 . Let $D = \{1,2,3,\ldots,k\}$ is set of colors with k colors and c_7 is function who pairing every vertex and edges to set of color $D, c_7 \colon (V(Shack(B_2,v,n)) \cup E(Shack(B_2,v,n))) \to D$. Coloring function c_7 is as follows:

$$c_7(x_{ij}) = \begin{cases} 4, \ 1 \leq i \leq n, \ j = 1 \\ 3, \ 1 \leq i \leq n, \ j = 2 \end{cases}$$

$$c_7(z_{ij}) = \begin{cases} 6, \ 1 \leq i \leq n, \ j = 1 \\ 8, \ 1 \leq i \leq n, \ j = 2 \end{cases}$$

$$c_7(y_i) = 1, 1 \leq i \leq n, \ j = 2$$

$$c_7(y_i) = 1, 1 \leq i \leq n, \ j = 1$$

$$c_7(x_{ij}y_i) = 9, 1 \leq i \leq n, \ j = 1$$

$$c_7(x_{ij}y_{i+1}) = 10, 1 \leq i \leq n, \ j = 2$$

$$c_7(y_iz_{ij}) = 2, 1 \leq i \leq n, \ j = 1$$

$$c_7(y_{i+1}z_{ij}) = 5, 1 \leq i \leq n, \ j = 1$$

$$c_7(x_{ij}z_{ij+1}) = 3, 1 \leq i \leq n, \ j = 1$$

$$c_7(x_{ij}z_{ij+1}) = 4, 1 \leq i \leq n, \ j = 1$$

$$c_7(z_{ij}z_{ij+1}) = 7, 1 \leq i \leq n, \ j = 1$$

Of coloring function on c_7 It is evident that the chromatic number total of *shackle* book graph, $G=(Shack(B_2,v,n))$ is $\chi_6''(G)\leq 10$. Since $\chi_6''(G)\leq 10$ and $\chi_6''(G)\geq 10$ then $\chi_6''(G)=10$ so chromatic number $\chi_5''(G)=10$.

On graph operating shackle book graph B_2 , if in terms of coloring the vertex is, number of $\min\{r, \max\{d(v) + |(N(v))|\}\} = \max\{d(z_{ij}) + |(N(z_{ij}))|\} = 8$. In the the edge of on operation graph shackle book graph B_2 , number of $\min\{r, \max\{d(u) + d(v)\}\} = \max\{d(u) + d(v)\} = 7$, resulting in $\chi''_{r\geq 6}(Shack(B_2, v, n)) = 10$. This is because when $r \geq 6$ number $\min\{r, \max\{d(v) + |(N(v))|\}\} = \max\{d(z_{ij}) + |(N(z_{ij}))|\} = 6$ and number $\min\{r, \max\{d(u) + d(v)\}\} = \max\{d(u) + d(v)\} = 7$. From the above description, so Theorem 2 proven. \square

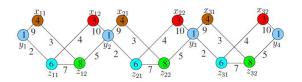


Fig 4. Total r-dynamic Coloring on Graph $Shack(B_2, v, n)$

 \Diamond **Theorem 3.** Let graph G is operation graph shackle of graph cocktail party $H_{2,2}$. For $n \geq 2$, chromatic number total r-dynamic graph $Shack(H_{2,2}, v, n)$ is

$$\chi_r''(shack(H_{2,2},v,n)) = \begin{cases} & 5 \text{ untuk } 1 \leq r \leq 3 \\ & 7, \text{ untuk } 4 \leq r \leq 5 \\ & 10, \text{ untuk } 6 \leq r \leq 7 \\ & 11, \text{ untuk } r \geq 8 \end{cases}$$

Proof. Set of vertices of graph $V(Shack(H_{2,2},v,n))=\{x_i; 1\leq i\leq n+1\}\cup\{y_i,z_i; 1\leq i\leq n\}$ and set of edges

 $E(H_{2,2}, v, n)) = \{x_i x_{i+1}; 1 \le i \le n\} \cup \{x_i z_i; 1 \le i \le n\}$ $n\} \cup \{y_i x_{i+1}; 1 \le i \le n\} \cup \{y_i z_i; 1 \le i \le n\}.$ So cardinality vertex and edges is $|V(Shack(H_{2,2}, v, n))| =$ 3n + 1 and $|E(Shack(H_{2,2}, v, n))| = 4n$, and $\Delta(G) = 4$. Case 1. Based on Conjecture 1 that $\Delta(G) + 1 \leq$ $\chi_r''(G) \leq \Delta(G) + 2$, so $\chi''(Shack(H_{2,2}, v, n)) \geq 5$. To prove the chromatic number total 1,2,3-dynamic coloring of graph $(Shack(H_{2,2}, v, n))$ is 5, needs to be proven $\chi''(Shack(H_{2,2}, v, n)) \ge$ 5 and $\chi''(Shack(H_{2,2},v,n)) \le 5$. Then indicated that the chromatic number $\chi''(Shack(H_{2,2},v,n)) \le 5$ by coloring function c_{10} . Let $D = \{1, 2, 3, \dots, k\}$ is the set of color with k colors and c_{10} is function who pairing every vertices and edges to the set of color D, c_{19} : $(V(Shack(H_{2,2}, v, n)) \cup E(Shack(H_{2,2}, v, n))) \rightarrow D.$ Coloring function c_{10} is as follows:

$$c_{10}(x_i) = \begin{cases} 1, \ 1 \le i \le n+1, \\ i \equiv 1 \pmod{3} \end{cases}$$

$$c_{10}(x_i) = \begin{cases} 3, \ 1 \le i \le n+1, \\ i \equiv 2 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n+1, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 1, \ 1 \le i \le n, \\ i \equiv 1 \pmod{3} \end{cases}$$

$$c_{10}(y_i) = \begin{cases} 3, \ 1 \le i \le n, \\ i \equiv 2 \pmod{3} \end{cases}$$

$$\begin{cases} 3, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 3, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$c_{10}(z_i) = \begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 2 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 2, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 3, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

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$$\begin{cases} 3, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 3, \ 1 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

Of coloring function on c_{10} tt is evident that the chromatic number total *shackle* graph *cocktail party* $H_{2,2}$,

On Total r-Dynamic Coloring of Several Classes of Graphs and Their Related Operations



illustration, served Figure 7 who is 1,2,3-dynamic coloring *shackle* graph *cocktail party* $H_{2,2}$.

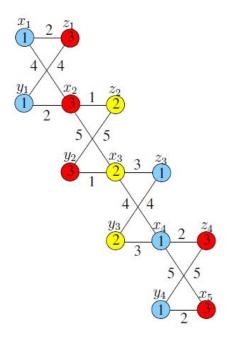


Fig 5. Total 1,2,3-dynamic Coloring on Graph $Shack(H_{2,2},v,n)$

Case 2. Based on Observation [1] that $\chi_4''(G) \geq \chi_3''(G)$, Can be concluded $\chi_4''(Shack(H_{2,2},v,n)) \geq \chi_3''(Shack(H_{2,2},v,n))$. Let $\chi_4''(Shack(H_{2,2},v,n)) = 5$ As on coloring function c_{10} , So does not meet the definition total r-dynamic coloring. So that required the addition of color become 6-coloring, $\chi_4''(Shack(H_{2,2},v,n)) \geq 6$. But with 6-coloring still not meet total r-dynamic coloring, so that plus to 7 coloring, then $\chi_4''(Shack(H_{2,2},v,n)) \geq 7$.

To prove chromatic numbers of the total 4-dynamic coloring on graph $Shack(H_{2,2},v,n)$ is 7, needs to be proven $\chi_4''(Shack(H_{2,2},v,n)) \geq 7$ and $\chi_4''(Shack(H_{2,2},v,n)) \leq 7$. Then indicated that the chromatic number $\chi_4''(Shack(H_{2,2},v,n)) \leq 7$ by coloring function c_{11} . Let $D=\{1,2,3,\ldots,k\}$ is set of colors with k colors and c_{11} is function who pairing every vertex and edges to set of color $D, c_{11}: (V(Shack(H_{2,2},v,n)) \cup E(Shack(S_5,v,n))) \rightarrow D$. Coloring function c_{11} is as follows:

$$c_{11}(z_i) = \begin{cases} 3, \ 1 \leq i \leq n, \\ i \equiv 1 \pmod{3} \end{cases}$$

$$c_{11}(z_i) = \begin{cases} 2, \ 1 \leq i \leq n, \\ i \equiv 2 \pmod{3} \end{cases}$$

$$5, \ 1 \leq i \leq n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\begin{cases} 1, \ i = 1 \\ 5, \ 2 \leq i \leq n+1, \\ i \equiv 2 \pmod{3} \end{cases}$$

$$c_{11}(x_i) = \begin{cases} 3, \ 2 \leq i \leq n+1, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$\vdots$$

$$c_{12}(x_i) = \begin{cases} 3, \ 2 \leq i \leq n+1, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$c_{11}(x_i z_i) = \begin{cases} 2, i = 1 \\ 3, 2 \le i \le n, \\ i \equiv 2 \pmod{3} \end{cases}$$

$$c_{11}(x_i z_i) = \begin{cases} 2, 2 \le i \le n, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$c_{11}(y_i) = \begin{cases} 4, 1 \le i \le n, i \text{ odd} \\ 1, 1 \le i \le n, i \text{ even} \end{cases}$$

$$c_{11}(x_i x_{i+1}) = \begin{cases} 6, 1 \le i \le n, i \text{ odd} \\ 7, 1 \le i \le n, i \text{ even} \end{cases}$$

$$c_{11}(y_i z_i) = \begin{cases} 7, 1 \le i \le n, i \text{ odd} \\ 6, 1 \le i \le n, i \text{ even} \end{cases}$$

$$c_{11}(y_i z_i) = \begin{cases} 7, 1 \le i \le n, i \text{ odd} \\ 6, 1 \le i \le n, i \text{ even} \end{cases}$$

$$c_{11}(y_i x_{i+1}) = \begin{cases} 1, 1 \le i \le n, i \text{ odd} \\ 4, 1 \le i \le n, i \text{ even} \end{cases}$$

Of coloring function on c_{11} It is evident that the chromatic number total shackle graph cocktail party $H_{2,2}$ is $\chi''(Shack(H_{2,2},v,n)) \leq 7$. Since chromatic number $\chi''(Shack(H_{2,2},v,n)) \leq 7$ and $\chi''(Shack(H_{2,2},v,n)) \geq 7$ Can be concluded $\chi''(Shack(H_{2,2},v,n)) = 7$ so $\chi''_4(Shack(H_{2,2},v,n)) = \chi''_5(Shack(H_{2,2},v,n)) = 7$.

Case 3. Based on Observation 1 that $\chi_6''(G) \geq \chi_5''(G)$, can be concluded $\chi_6''(Shack(H_{2,2},v,n)) \geq \chi_5''(Shack(H_{2,2},v,n))$. Let $\chi_6''(Shack(H_{2,2},v,n)) = 7$ as on coloring function c_{11} , so does not meet definition of total r-dynamic coloring. so that required the addition of colors become 8-coloring, $\chi_6''(Shack(H_{2,2},v,n)) \geq 8$. But with 78 coloring still not meet total r-dynamic coloring, so that plus to 9 coloring, then chromatic number $\chi_6''(Shack(H_{2,2},v,n)) \geq 9$.

To prove chromatic numbers of the total 6-dynamic coloring on graph $Shack(H_{2,2},v,n)$ is 9, needs to be proven $\chi_6''(Shack(H_{2,2},v,n)) \geq 9$ and $\chi_6''(Shack(H_{2,2},v,n)) \leq 9$. Then indicated that the chromatic number $\chi_6''(Shack(H_{2,2},v,n)) \leq 9$ by coloring function c_{12} . Let $D=\{1,2,3,\ldots,k\}$ is set of colors with k colors and c_{12} is function who pairing every vertex and edges to set of color $D, c_{12}: (V(Shack(H_{2,2},v,n)) \cup E(Shack(H_{2,2},v,n))) \rightarrow D$. Coloring function c_{12} is as follows:

$$c_{12}(x_i) = \begin{cases} 1, \ 1 \le i \le n+1, \ i \text{ odd} \\ 6, \ 1 \le i \le n+1, \ i \text{ even} \end{cases}$$

$$c_{12}(y_i) = \begin{cases} 4, \ 1 \le i \le n, \ i \text{ odd} \\ 5, \ 1 \le i \le n, \ i \text{ even} \end{cases}$$

$$c_{12}(z_i) = \begin{cases} 3, \ 1 \le i \le n, \ i \text{ odd} \\ 2, \ 1 \le i \le n, \ i \text{ even} \end{cases}$$

$$c_{12}(x_iz_i) = \begin{cases} 2, \ 1 \le i \le n, \ i \text{ odd} \\ 3, \ 1 \le i \le n, \ i \text{ even} \end{cases}$$

$$c_{12}(x_ix_{i+1}) = \begin{cases} 7, \ 1 \le i \le n, \ i \text{ odd} \\ 9, \ 1 \le i \le n, \ i \text{ even} \end{cases}$$

$$c_{12}(y_ix_{i+1}) = \begin{cases} 5, \ 1 \le i \le n, \ i \text{ odd} \\ 4, \ 1 \le i \le n, \ i \text{ even} \end{cases}$$

$$c_{12}(y_iz_i) = 8, 1 \le i \le n$$

Of coloring function on c_{12} It is evident that the chromatic number total shackle graph cocktail $party\ H_{2,2}$ is $\chi_6''(Shack(H_{2,2},v,n)) \le 9$. Since chromatic number $\chi_6''(Shack(H_{2,2},v,n)) \le 9$ and $\chi_6''(Shack(H_{2,2},v,n)) \ge 9$ can be concluded $\chi_6''(Shack(H_{2,2},v,n)) = 9$ so $\chi_6''(Shack(H_{2,2},v,n)) =$



 $\chi_7''(Shack(H_{2,2}, v, n)) = 9.$

Case 4. Based on Observation [1] that $\chi_8''(G) \geq \chi_7''(G)$, can be concluded $\chi_8''(Shack(H_{2,2},v,n)) \geq \chi_7''(Shack(H_{2,2},v,n))$. Let $\chi_8''(Shack(H_{2,2},v,n)) = 9$ as on coloring function c_{12} , So does not meet definition of total r-dynamic coloring. So that required the addition of colors become 10-coloring, $\chi_8''(Shack(H_{2,2},v,n)) \geq 10$. But with 10-coloring still not meet total r-dynamic coloring, so that plus to 11-coloring, then $\chi_8''(Shack(H_{2,2},v,n)) \geq 11$.

To prove chromatic numbers of the total 8-dynamic coloring on graph $G = Shack(H_{2,2},v,n)$ is 11, needs to be proven $\chi_8''(G) \geq 11$ and $\chi_8''(G) \leq 11$. Then indicated that the chromatic number $\chi_8''(G) \leq 11$ by coloring function c_{13} . Let $D = \{1,2,3,\ldots,k\}$ is set of colors with k colors and c_{13} is function who pairing every vertex and edges to set of color $D, c_{13} : V(Shack(H_{2,2},v,n)) \cup E(Shack(H_{2,2},v,n)) \rightarrow D$. Coloring function c_{13} is sa follows:

$$\begin{cases} 1, \ 1 \leq i \leq n+1, \\ i \equiv 1 \pmod{3} \end{cases}$$

$$c_{13}(x_i) = \begin{cases} 6, \ 1 \leq i \leq n+1, \\ i \equiv 2 \pmod{3} \end{cases}$$

$$\begin{bmatrix} 11, \ 1 \leq i \leq n+1, \\ i \equiv 0 \pmod{3} \end{cases}$$

$$c_{13}(y_i) = \begin{cases} 4, \ 1 \leq i \leq n, \ i \text{ odd} \\ 5, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

$$c_{13}(z_i) = \begin{cases} 3, \ 1 \leq i \leq n, \ i \text{ odd} \\ 2, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

$$c_{13}(x_iz_i) = \begin{cases} 2, \ 1 \leq i \leq n, \ i \text{ odd} \\ 3, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

$$c_{13}(x_ix_{i+1}) = \begin{cases} 5, \ 1 \leq i \leq n, \ i \text{ odd} \\ 4, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

$$\begin{cases} 7, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

$$\begin{cases} 7, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

$$\begin{cases} 7, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

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$$\begin{cases} 8, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

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$$\begin{cases} 10, \ 1 \leq i \leq n, \ i \text{ even} \end{cases}$$

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$$\begin{cases} 10, \ 1 \leq i \leq n, \text$$

Of coloring function on c_{13} it is evident that the chromatic number total *shackle* graph *cocktail party* $H_{2,2}$

is $\chi_8''(G) \leq 11$. Since $\chi_8''(G) \leq 11$ and $\chi_8''(G) \geq 11$ then $\chi_8''(G) = 11$ so $\chi_8''(G) = \chi_r''(G) = 11$. As illustratio, served Figure 8 who is r-dynamic coloring of shackle graph cocktail party $H_{2,2}$.

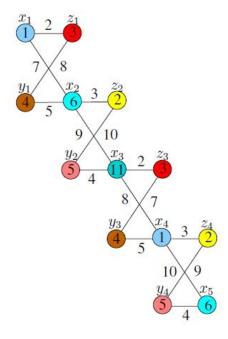


Fig 6. Total r-dynamic Coloring on Graph $Shack(H_{2,2}, v, n)$

On operation graph shackle graph cocktail party $(Shack(H_{2,2},v,n))$, if in terms of coloring the vertex is, number of $\min\{r,\max\{d(v)+|(N(v))|\}\}=\max\{d(x_i)+|(N(x_i))|\}=8$. In the the edge of on operation graph shackle graph cocktail party $H_{2,2}$. $(Shack(H_{2,2},v,n))$ number of $\min\{r,\max\{d(u)+d(v)\}\}=\max\{d(u)+d(v)\}=8$, resulting in $\chi''_{r\geq 8}(Shack(H_{2,2},v,n))=11$. From the above description, so Theorem $\mathbb B$ proven.

OPEN PROBLEM

Find the chromatic number of total r-dynamic coloring of special graph and operation graph shackle and $generalized\ shackle$ the other graph.

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